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## **PSYC214: Statistics** Lecture 5 – Summary Part 1

Michaelmas Term Dr Sam Russell s.russell1@lancaster.ac.uk

1





Within and between participant designs

2

# Lancaster 🎦 University **Experimental science** Population versus sample Population is every individual you are interested in • The sample is a subset of your

population of interest. We examine samples because it is typically impossible to sample everyone in the population



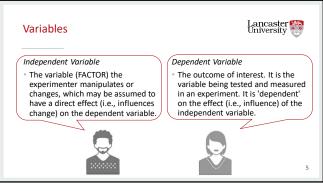
### **Experimental science**

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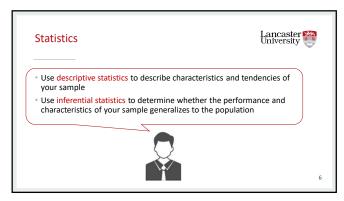
- Population versus sample
   You should always opt for
- random sampling, where you pick your sample randomly
- However, in reality, we often use opportunity sampling where we recruit who we have access to











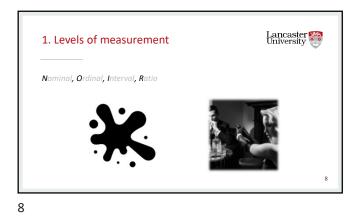


### **Descriptive statistics**

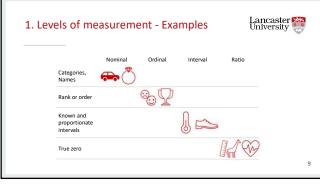
1. Levels of measurement

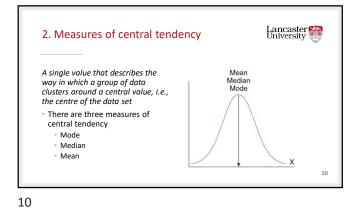
- 2. Measures of central tendency
- 3. Measures of variability

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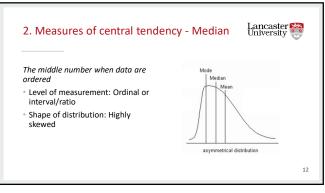
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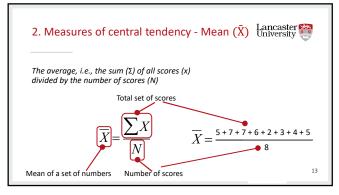


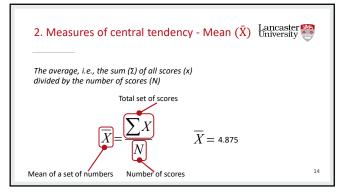




Lancaster 🤮 University 2. Measures of central tendency Nominal Ordinal Interval Ratio Mode, % frequenci Mode, % frequenci Mode, % frequenci Mode, % frequencies Categories, Names ries Median, percentile Median, percentile Median, percentile Rank or order Known and proportionate intervals Mean, standard deviation Mean, standard deviation All above True zero 11

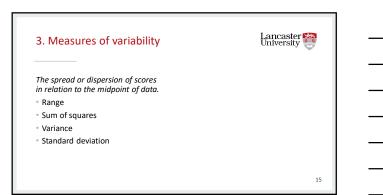


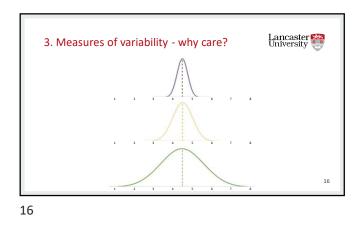




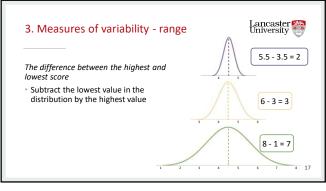






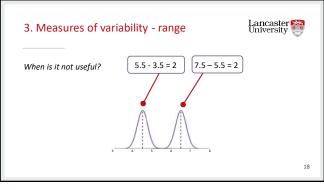




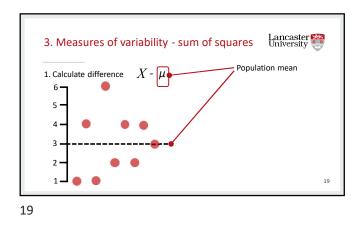




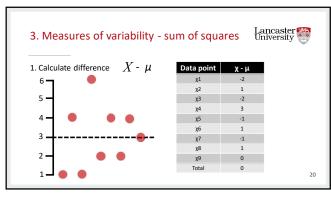






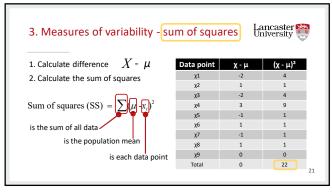




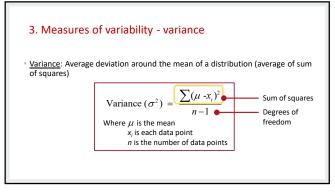


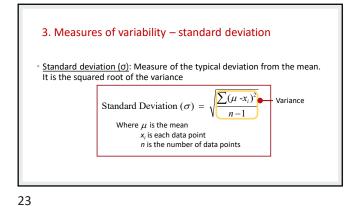


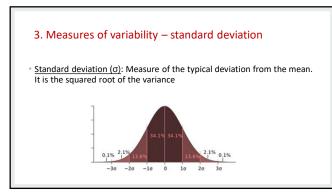












#### Inferential statistics

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- 1. Allow you to draw conclusions based on extrapolations
- 2. Use data from the sample of participants in the experiment to compare the treatment groups and make generalizations about the larger population of participants
- 3. Provide a quantitative method to decide if the null hypothesis  $({\rm H}_0)$  should be rejected

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#### Inferential statistics - Hypotheses



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Ho the Null Hypothesis

- Ho: there is no significant difference between the conditions/groups and the null hypothesis is accepted.
- Under H<sub>0</sub>, the samples come from the same population.

# H1 the Experimental Hypothesis

- Ha: there is a significant difference between the conditions/groups and the null hypothesis is rejected.
- Under H<sub>1</sub>, the samples come from the <u>different</u> populations.

<ul> <li>Statistical tests can be separated into: <ul> <li>Parametric</li> <li>Non-parametric</li> </ul> </li> <li>While parametric tests are the norm in psychology and are generally more powerful than non-parametric tests, they require that the scores be an interval or ratio measure and there needs to be homogeneity of variance</li> </ul>	Inferential statistics - (Non)parametric tests	Lancaster 🎇 University
<ul> <li>Non-parametric</li> <li>While parametric tests are the norm in psychology and are generally more powerful than non-parametric tests, they require that the scores be an</li> </ul>	<ul> <li>Statistical tests can be separated into:</li> </ul>	
While parametric tests are the norm in psychology and are generally more powerful than non-parametric tests, they require that the scores be an	- Parametric	
powerful than non-parametric tests, they require that the scores be an	- Non-parametric	
	powerful than non-parametric tests, they require that the sco	es be an

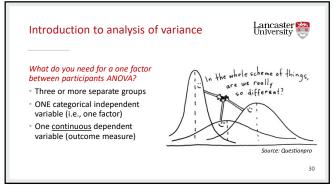


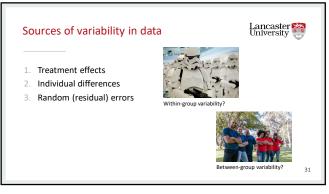




- Calculating within-group and betweengroup variances
- Degrees of Freedom
- Producing the F-statistic











### Random (residual) errors

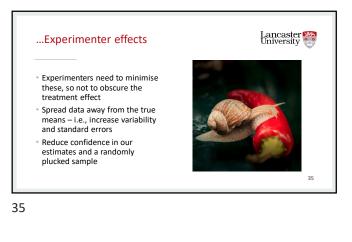
- Ideally a participant would have a 'true level' at which they perform, which can always be measured accurately
- 1. Varying external conditions e.g., temperature, time of day
- State of participant (e.g. tired?)
- Experimenter's ability to 3. measure accurately...

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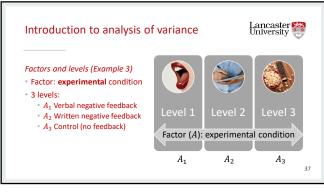
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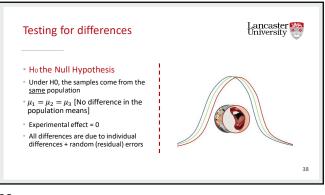


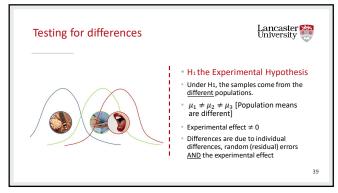
Between-group variability The extent to which overall groups differ from one another (hopefully because of our treatment) \* but also Individual differences!

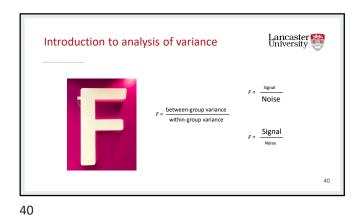




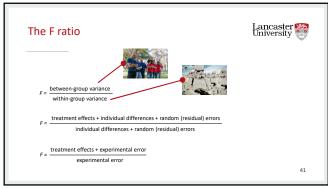


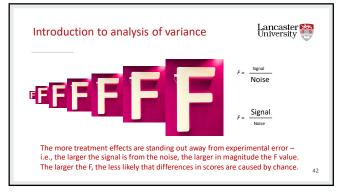




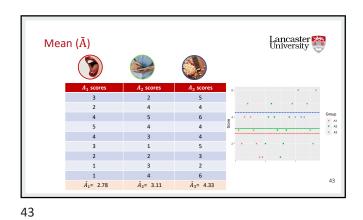




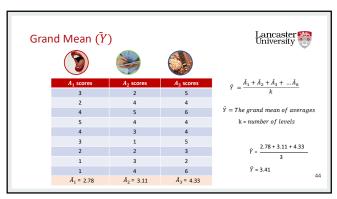




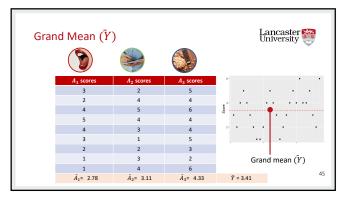


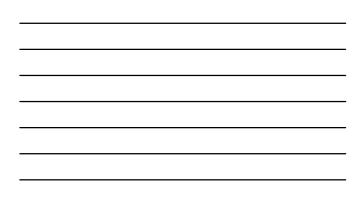


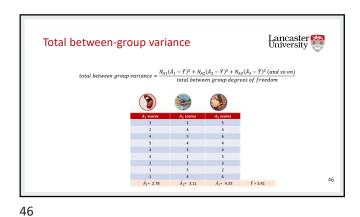


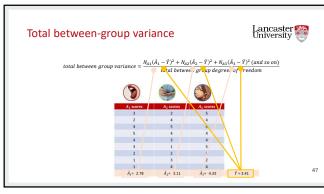






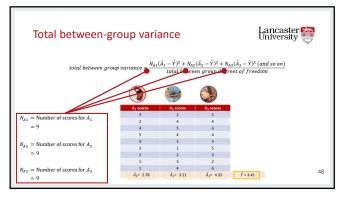




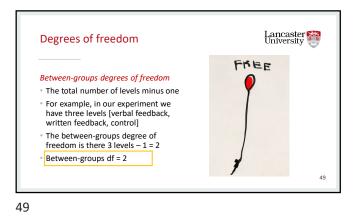


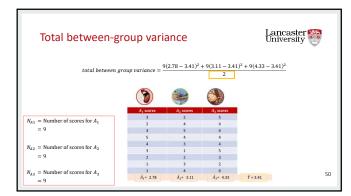


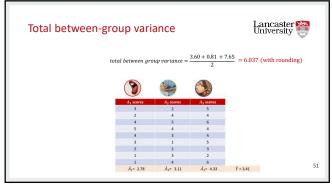






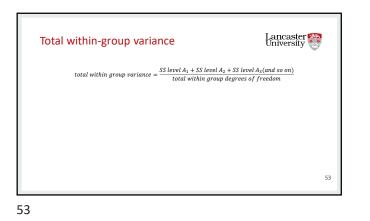


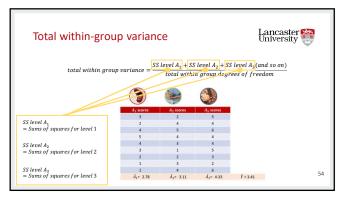


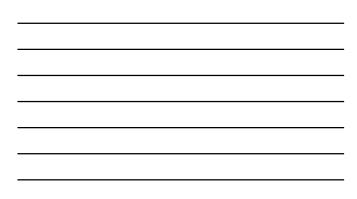


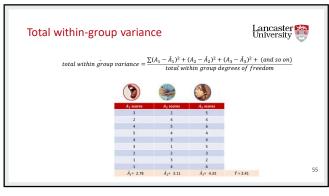




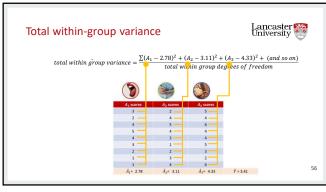


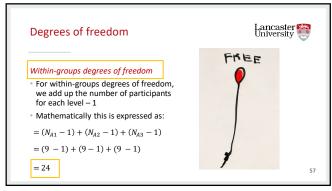




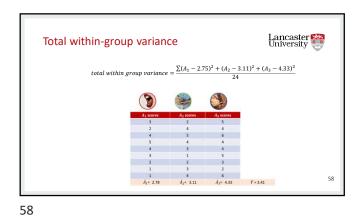


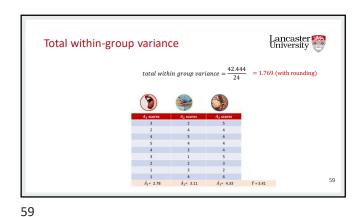




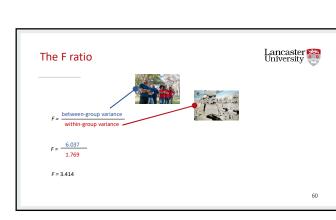




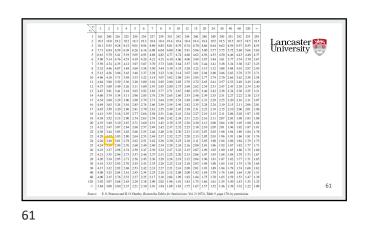




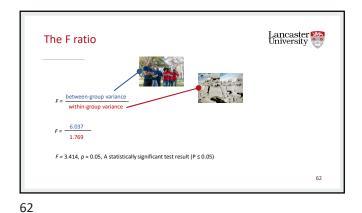


















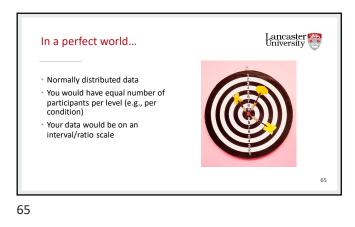
## Assumptions of ANOVA and follow-up procedures

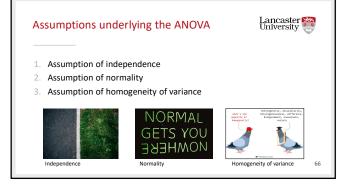
### Agenda/Content for Lecture 3

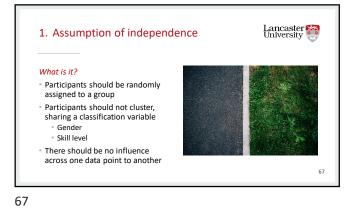
- Assumptions of ANOVA
  - Assumption of independence
     Assumption of normality
  - Assumption of homogeneity of variance
- Data transformations
- Pairwise between-level comparisons
   Planned comparisons
  - Post-hoc tests



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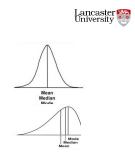


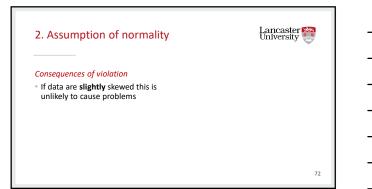


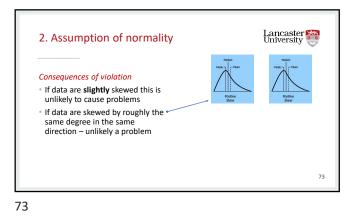


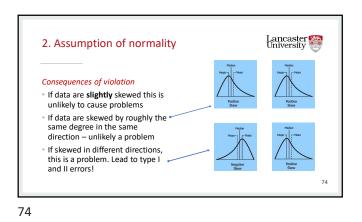
#### What is it?

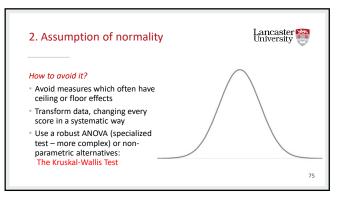
- You want the overall data and the data for each subgroup to normally distributed
- This is because ANOVAs rely on the mean – and for skewed and bimodal data the mean is unlikely the best measure of central tendency







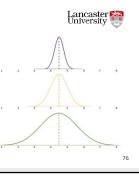




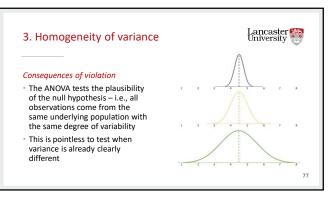
### 3. Homogeneity of variance



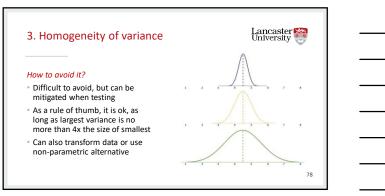
- Assumes that the variances of the distributions in the samples are equal
- Therefore the variances for each sample should not significantly vary from one another











## Dealing with 'rogue' data

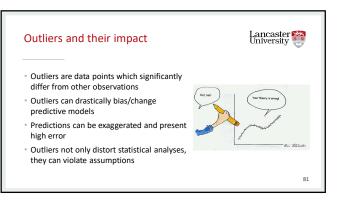
#### Transforming data

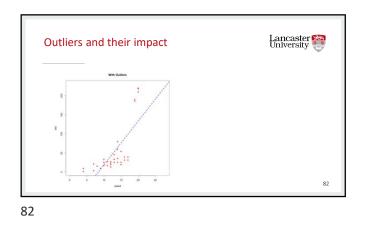
- This involves taking every score from each participant and applying a uniform mathematical function to each
- Report both the original data and the transformed data

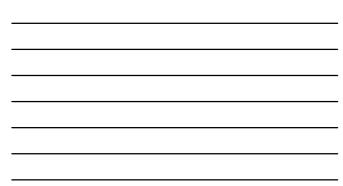
×,		$\bigcup_{X_i'=\log X_i}$
		X7 = accsin (X) <sup>2/2</sup>
	<del>.</del>	$X_{j}' = \log \frac{X_{j}}{1 - X_{j}}$
		$x_j = v_j \log \frac{1 + x_j}{1 - x_j}$
$X_j = \text{raw data distribution}$	1.	$x_j = \log \frac{x_j}{1 - x_j}$
$X_j^* \sim \text{transformed data distribution}$		X;- mode (X; <sup>16</sup>
x, Figure from Stever	ns (2002)	$X_j^* = \forall 2 \log \frac{1+X_j}{1-X_j}$

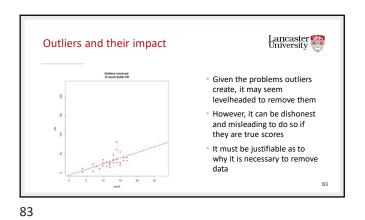


Dealing w	ith 'rog	ue' data		Lancaster University
			Type of Data Transformation	Nature of Data
How to trans	form data		Log Transformation	Whole numbers and cover wide range of values, small values
Untransformed	Square-root transformed	Log transformed		with decimal fractions.
38	6.164	1.580	$(\log(X_i))$	
1	1.000	0.000		
13	3.606	1.114	1	
2	1.414	0.301	1	
13	3.606	1.114		
	4-472	1.301	Square-root	Small whole number &
20	7.071	1.699	Transformation	Percentage data where
		0.954		the range is between
20 50 9	3.000		$(\sqrt{X_i})$	0 and 30 % or
20 50	5.292	1.447		between 70 and 100
20 50 9	5-292 2-449	0.778		
20 50 9	5.292			%

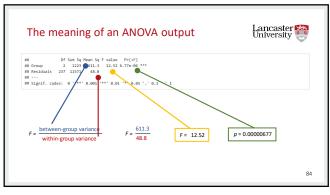




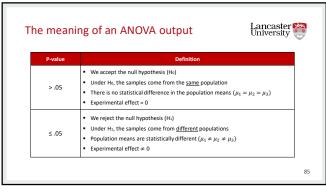


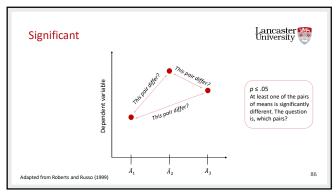


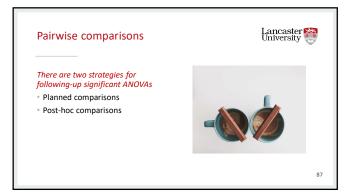














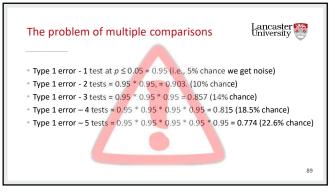


• Why not just run a bunch of t-tests?

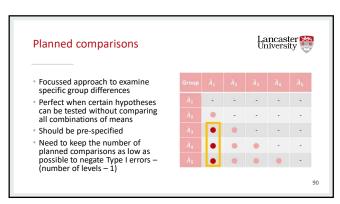
Multiple comparisons increase the probability of making a (familywise) type I error

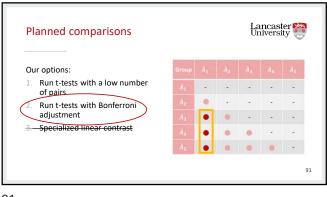
• I.e., rejecting the null hypothesis when actually there was no effect

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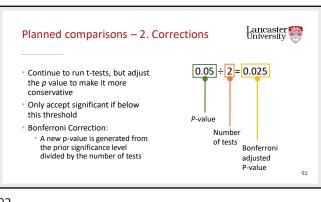


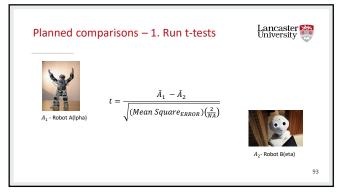
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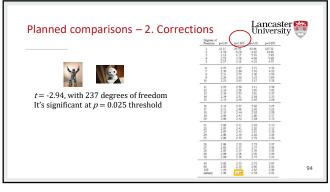


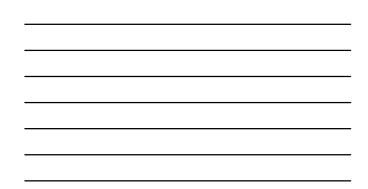


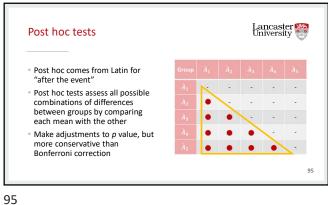




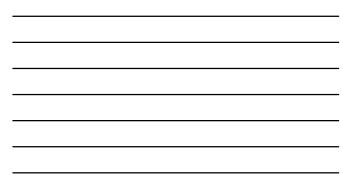


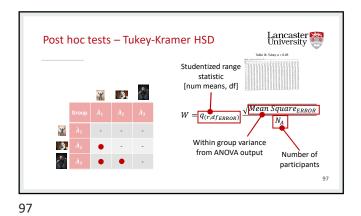




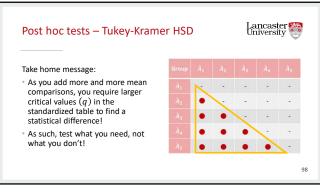


Post hoc tests Lanc					Lancaster University
Method	Equal N F	Normality	Use	Error control	Protection
Fisher PLSD	Yes	Yes	Yes	All	Most sensitive to Type 1
Tukey-Kramer HSD	No	Yes	Yes	All	Less sensitive to Type 1 than Fisher PLSD
Spjotvoll-Stoline	No	Yes	Yes	All	As Tukey-Kramer
Student-Newman Keuls (SNK)	Yes	Yes	Yes	All	Sensitive to Type 2
Tukey-Compromise	No	Yes	Yes	All	Average of Tukey and SNK
Duncan's Multiple Range	No	Yes	Yes	All	More sensitive to Type 1 than SNK
Scheffé's S	Yes	No	No	All	Most conservative
Games/Howell	Yes	No	No	All	More conservative than majority
Dunnett's test	No	No	No	T/C	More conservative than majority
Bonferroni	No	Yes	Yes	All, TC	Conservative

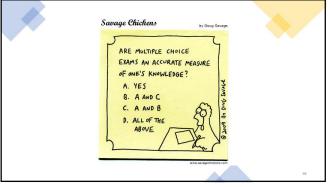












## One factor within-participants ANOVA

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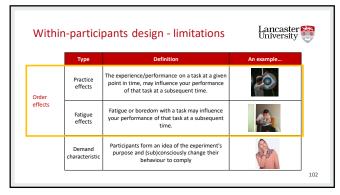
Agenda/Content for Lecture 4 • Introduction to one factor within-

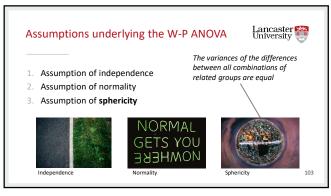
- Participants ANOVA and its limitations
   Between-participant variability and residual
- variance
- Calculating within-group and between group variances
- Producing the within-participants F-statistic

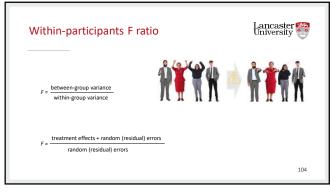


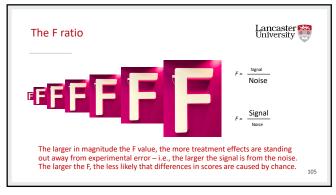
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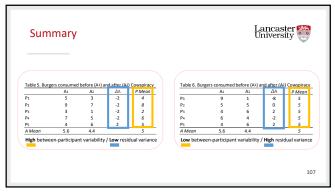


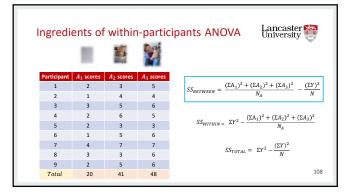




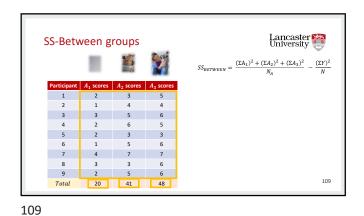






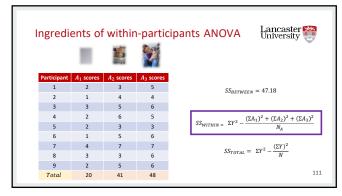




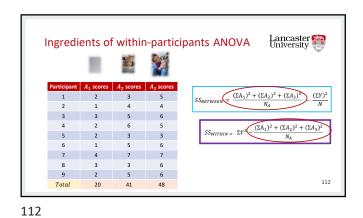




Lancaster 🎇 University 👹 SS-Between groups  $SS_{BETWEEN} = \frac{(\Sigma A_1)^2 + (\Sigma A_2)^2 + (\Sigma A_3)^2}{N_A} - \frac{(\Sigma Y)^2}{N}$  $SS_{BETWEEN} = \frac{(20)^2 + (41)^2 + (48)^2}{9} - \frac{(109)^2}{27}$ A<sub>1</sub> scores A<sub>2</sub> scores A<sub>3</sub> so  $SS_{BETWEEN} = \frac{400 + 1681 + 2304}{9} - \frac{11881}{27}$ 5 6  $SS_{BETWEEN} = 44.44 + 186.77 + 256.00 - 440.03$ SS<sub>BETWEEN</sub> = 487.21 - 440.03 SS<sub>BETWEEN</sub> = 47.18 Total 20 41 48







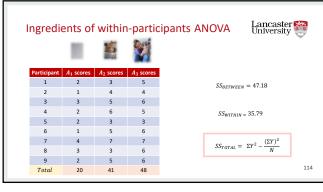


Lancaster 🤮 University SS-Within group Ħ  $SS_{WITHIN} \underbrace{(\Sigma A_{2})^{2} + (\Sigma A_{2})^{2} + (\Sigma A_{3})^{2}}_{N_{A}}$ A.2 SC A.,2 SCC 
 $A_2$  scores
  $A_2$  scores
  $A_2$  scores

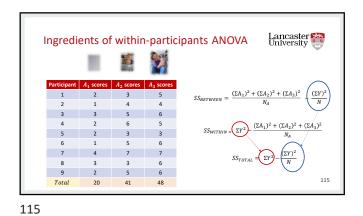
  $2^2$  4  $3^2$  9  $5^2$  25 

  $1^2$  4  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  16  $4^2$  1  $(20)^2 + (41)^2 + (48)^2$ SS<sub>WITHIN</sub> = 523 -3 9 4 400 + 1681 + 2304 SS<sub>WITHIN =</sub> 523 -9 6 7  $SS_{WITHIN} = 523 - 487.21$  $SS_{WITHIN} = 35.79$ 9 113 Total 20 41 48











Lancaster 🎇 University 😁 SS-Total  $SS_{TOTAL} = \Sigma Y^2 - \frac{(\Sigma Y)^2}{N}$ t A.2 sco A<sub>2<sup>2</sup></sub> scor A ... 2 SC 2<sup>2</sup> = 4 3<sup>2</sup> = 9 5<sup>2</sup> = 25 1  $SS_{TOTAL} = 523 - \frac{(109)^2}{27}$ 1<sup>2</sup> = 1 4<sup>2</sup> = 16 4² = 16 3² = 9  $5^2 = 25$   $6^2 = 36$  $6^2 = 36$   $5^2 = 25$ 3  $SS_{TOTAL} = 523 - \frac{11881}{27}$  $2^2 = 4$  $\begin{array}{c} 3^3 = 9 \\ 5^2 = 25 \quad 6^2 = 36 \\ 4^3 = 16 \quad 7^2 = 49 \quad 7^2 = 49 \\ 3^2 = 9 \quad 3^2 = 9 \quad 6^2 = 36 \\ 2^2 = 4 \quad 5^2 = 25 \quad 6^2 = 36 \\ 20 \quad 41 \quad 48 \end{array}$ 2<sup>2</sup> = 4 3<sup>2</sup> = 9 3² = 9 6 *SS<sub>TOTAL</sub>* = 523 - 440.03 7 *SS<sub>TOTAL</sub>* = 82.97 9 116 Total

